



DAKOTA 101: Wrap-Up

<http://dakota.sandia.gov>



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DAKOTA 101: Wrap-Up Topics



- **Review of DAKOTA's scope and relevance**
- **Recommended best practices**
- **Sneak preview of advanced topics**
 - Application interfacing
 - Parallelism
 - Hybrid and advanced algorithms
 - Parameter estimation
- **Resources for getting started**



DAKOTA Supports



DAKOTA includes a wide array of algorithm capabilities to support engineering transformation through advanced modeling and simulation.

- **Simulation-based engineering design: optimize virtual (computational) prototypes**
- **Risk analysis and quantification of margins and uncertainty (QMU): assess the effect of parametric uncertainty on the probability of achieving desired system performance**
- **Verification and validation: automate mesh convergence or solver tolerance studies, generate ensembles of possible simulations or statistics to compare to experimental data**

DAKOTA Explores Model Parameter Space to Answer Engineering Questions

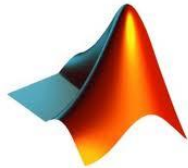


disease kinetic
parameters



epidemic size,
duration, severity

Matlab ODE
Epidemic
Model



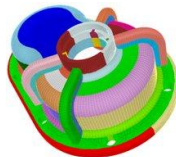
What are the crucial factors/parameters and how do they affect key metrics? (*sensitivity*)

material props,
boundary, initial
conditions



temperature,
stress, flow rate

Abaqus,
Sierra, CM/
CFD Model



How safe, reliable, robust, or variable is my system in the presence of uncertainties? (*UQ*)

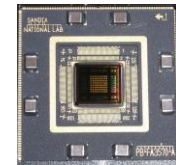
What models and parameters best match experimental data? (*calibration*)

resistances,
via diameters



voltage drop, peak
current

Xyce, Spice
Circuit
Model



What is the best performing design or control? (*optimization*)

load,
modulus



stress,
displacement

Cantilever
Beam Model

Basic Steps to Using DAKOTA



1. Define analysis goals; understand how DAKOTA helps and select a method to use
2. Access DAKOTA and understand help resources
3. **Workflow:** create an automated workflow so DAKOTA can communicate with your simulation (Advanced Topic)
 - Parameters to model, responses from model to DAKOTA
 - Typically requires scripting (Python, Perl, Shell, Matlab) or programming (C, C++, Java, Fortran)
 - Workflow usually crosscuts DAKOTA analysis types
4. **DAKOTA input file:** Jaguar GUI or text editor to configure DAKOTA to exercise the workflow to meet your goals
 - Tailor variables, methods, responses to analysis goals
5. Run DAKOTA: command-line; text input / output



Recommended Best Practices



- **Test the building blocks**
 - Test response extraction and interfaces before using with DAKOTA
 - Do a parameter study with a simple model
- **Start with a parameter study**
 - Screen problem characteristics: failure, smoothness, cost
 - Assess simulation robustness, verification, validity with respect to parameter variations
- **Solicit expert help in**
 - Formulating problem
 - Selecting appropriate methods
- **Question the numbers**
 - Sanity check aggregate/summary stats and results with more in-depth analyses of dakota-generated data.



Discussion: DAKOTA Relevance Revisited



- **Discuss your revised impressions of DAKOTA's relevance for your problems**
- **With what kinds of applications, simulations, computational models would you use it**
- **On what kinds of computer architecture would you want to use it (desktop workstation, Windows laptop, high-performance compute cluster)**

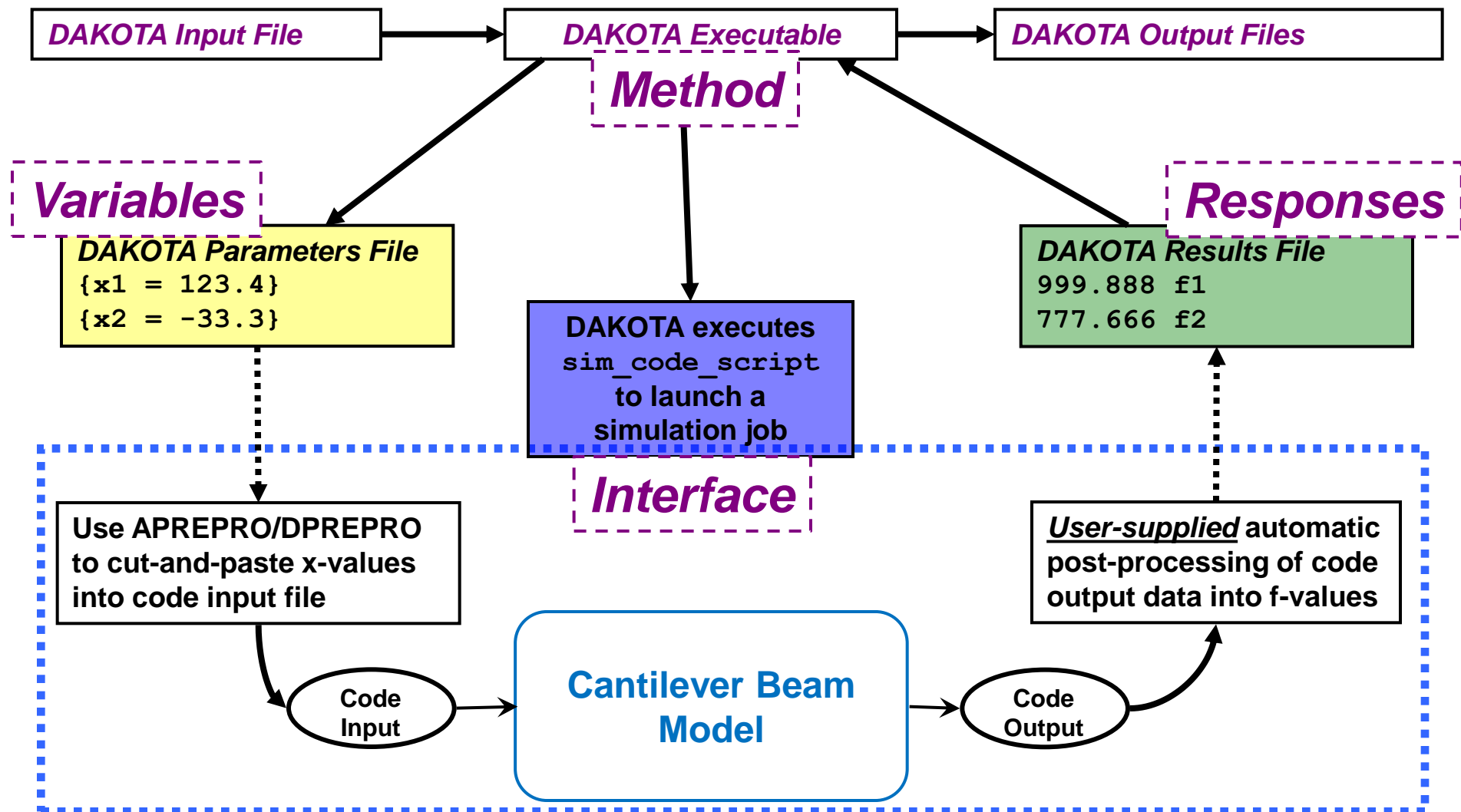


Sneak Preview of Advanced Topics



- **Application interfacing**
 - Generic interface to simulations
 - Parameters in, responses out
- **Parallelism**
 - Computing on multi-core desktops, clusters, and capability platforms
 - Different levels of parallelism
- **Hybrid and advanced algorithms**
 - Time-tested and advanced algorithms
 - Strategies for combining methods
- **Parameter Estimation**
 - Additional problem formulations
 - Future capabilities
 - User requirements

Interface communicates through file system and user-supplied script



Parallelism from a computing platform perspective

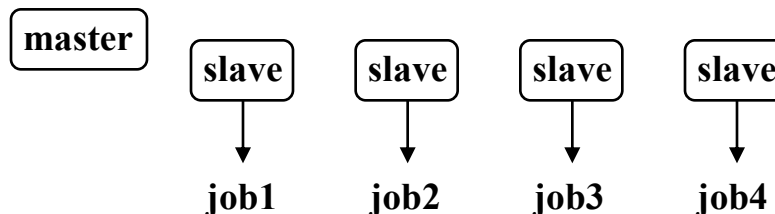


Nested parallel models support large-scale applications and architectures.

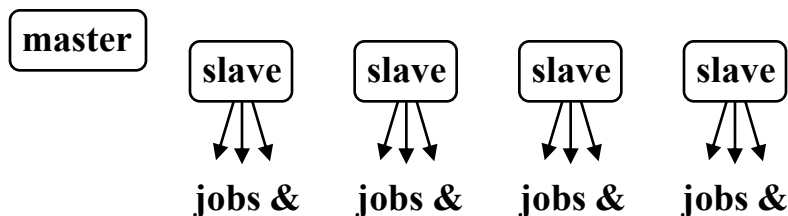
1. SMP/multiprocessor workstations: Asynchronous (external job allocation)



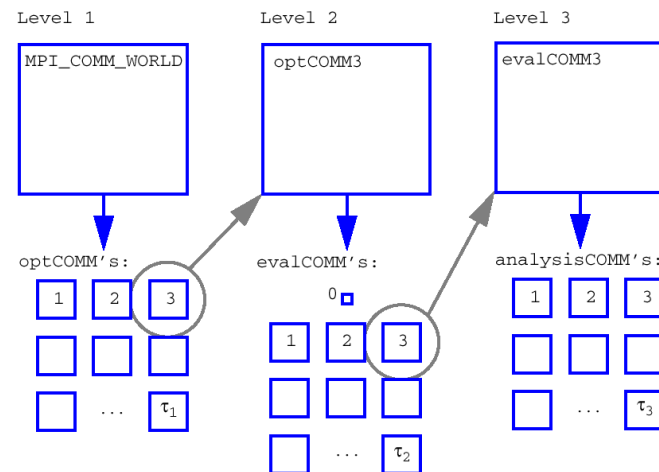
2. Cluster of workstations: Message-passing (internal job allocation)



3. Cluster of SMP's: Hybrid (service/compute model)



4. MPP: Internal MPI partitions (nested parallelism)



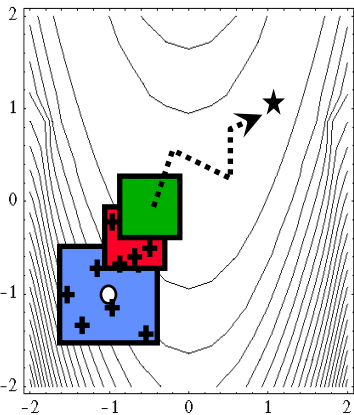


Parallelism from an algorithmic perspective



1. ***Algorithmic coarse-grained parallelism***: independent fn. Evaluations performed concurrently:
 - Gradient-based (e.g., finite difference gradients, speculative opt.)
 - Nongradient-based (e.g., GAs, PS, Monte Carlo)
 - Approximate methods (e.g., DACE)
 - Concurrent-method strategies (e.g., parallel B&B, island-model GAs, OUU)
2. ***Algorithmic fine-grained parallelism***: computing the internal linear algebra of an opt. algorithm in parallel (e.g., large-scale opt., SAND)
3. ***Function evaluation coarse-grained parallelism***: concurrent execution of separable simulations within a fn. eval. (e.g., multiple loading cases)
4. ***Function evaluation fine-grained parallelism***: parallelization of the solution steps within a single analysis code (e.g., SALINAS, MPSalsa)

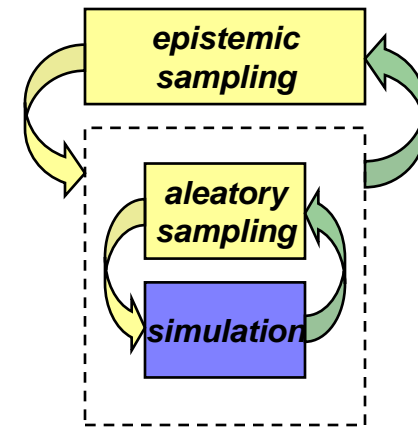
Opportunities for Mixing and Matching Methods



Strategies (general nesting, layering, sequencing and recasting facilities) **combine methods to enable advanced studies:**

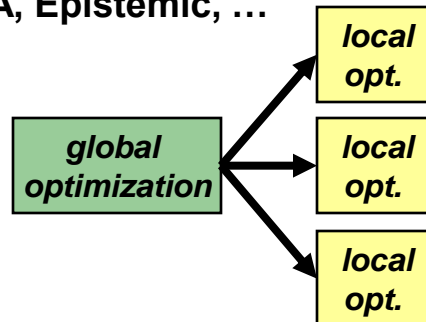
- opt within opt (multilevel opt & hierarchical MDO)
- UQ within UQ (second-order probability)
- UQ within opt (OUU) and NLS (MCUU)
- opt within UQ (uncertainty of optima)

with and without surrogate model indirection



Optimization

- Surrogate-based: data fit, multifidelity, ROM
- Mixed integer nonlinear programming (MINLP): PEBBL (parallel branch and bound)
- Optimization under uncertainty
 - TR-SBOUU, RBDO (Bi-level, Sequential)
 - MCUU, PC-BDO, EGO/EGRA, Epistemic, ...
- Hybrids (e.g., global/local)
- Pareto set
- Multi-start
- Multilevel methods



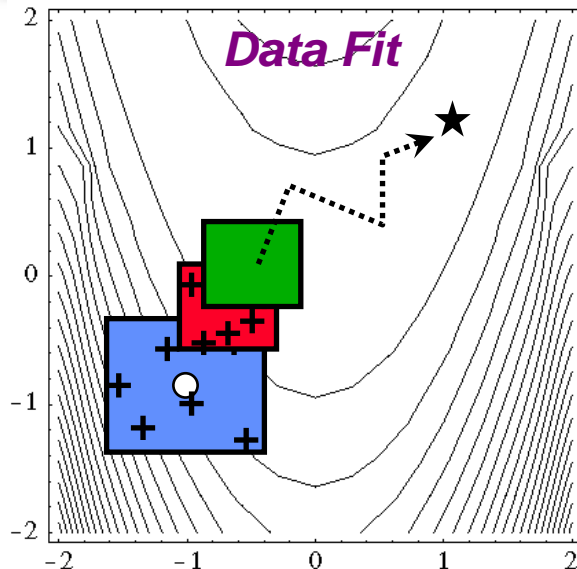
Uncertainty

- Second order probability
- Uncertainty of optima

Nonlinear least squares

- Surrogate-based calibration
- Model calibration under uncertainty

Trust Region Surrogate-Based Minimization

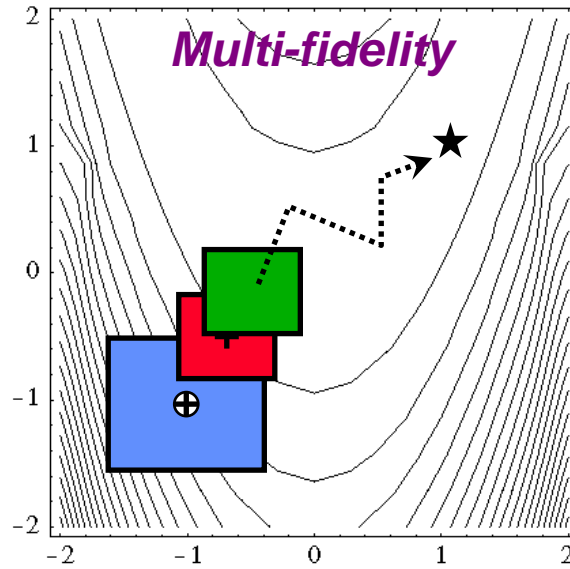


Data fit surrogates

- Global: polynomials, splines, neural network, Kriging, RBFs
- Local: 1st/2nd-order Taylor

Data fits in SBO

- Smoothing: extract global trend
- DACE: limited # design vars
- Must balance local consistency with global accuracy

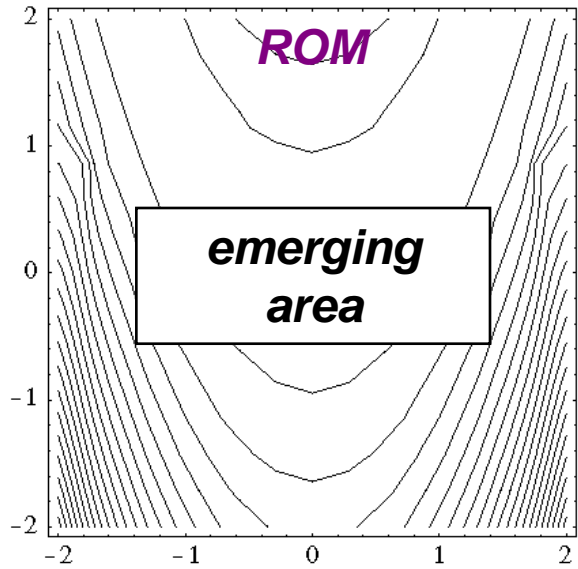


Multifidelity surrogates:

- Coarser discretizations, looser conv. tols., reduced element order
- Omitted physics: e.g., Euler CFD, panel methods

Multifidelity SBO

- HF scale better w/ des. vars.
- Requires smooth LF model
- May require design mapping
- Correction quality is crucial



ROM surrogates:

- Spectral decomposition
- POD/PCA w/ SVD
- KL/PCE (random fields, stochastic processes)

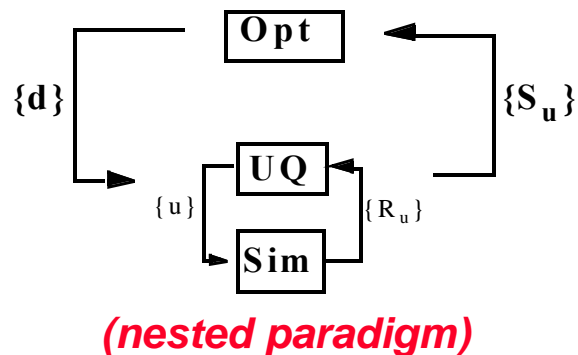
ROMs in SBO

- Key issue: parametrize (extended or spanning ROM)
- Otherwise like data fit case

Optimization Under Uncertainty



Rather than design and then post-process to evaluate uncertainty...
actively design optimize while accounting for uncertainty/reliability metrics
 $s_u(d)$, e.g., mean, variance, reliability, probability:

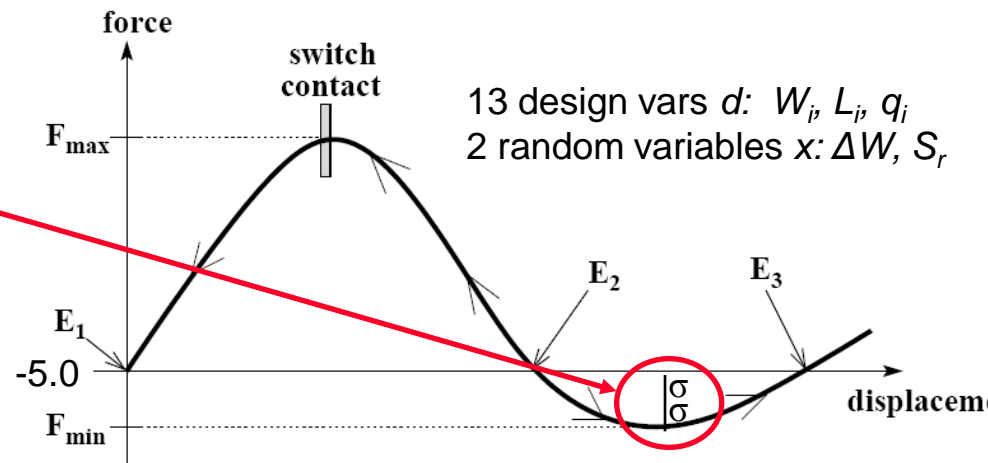


$$\begin{aligned}
 \min \quad & f(d) + W s_u(d) \\
 \text{s.t.} \quad & g_l \leq g(d) \leq g_u \\
 & h(d) = h_t \\
 & d_l \leq d \leq d_u \\
 & a_l \leq A_i s_u(d) \leq a_u \\
 & A_e s_u(d) = a_t
 \end{aligned}$$

Bistable switch problem formulation (Reliability-Based Design Optimization):

simultaneously reliable and robust designs

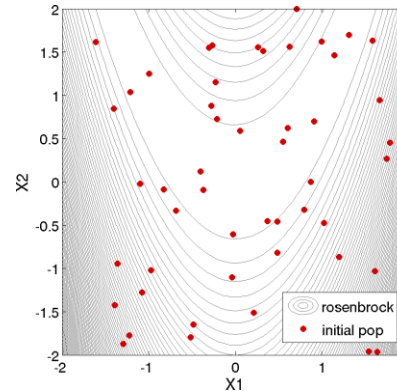
$$\begin{aligned}
 \max \quad & E[F_{min}(d, x)] \\
 \text{s.t.} \quad & 2 \leq \beta_{ccdf}(d) \\
 & 50 \leq E[F_{max}(d, x)] \leq 150 \\
 & E[E_2(d, x)] \leq 8 \\
 & E[S_{max}(d, x)] \leq 3000
 \end{aligned}$$



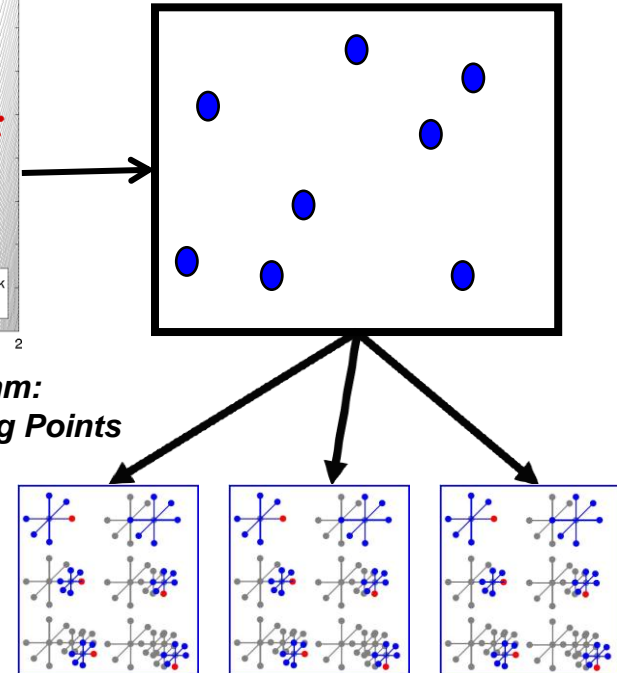
Hybrid Optimization



```
strategy,
  graphics
  hybrid sequential
  method_list = 'GA' 'PS' 'NLP'
method,
  id_method = 'GA'
  model_pointer = 'M1'
coliny_ea
  seed = 1234
  population_size = 10
  verbose output
method,
  id_method = 'PS'
  model_pointer = 'M1'
coliny_pattern_search stochastic
  seed = 1234
  initial_delta = 0.1
  threshold_delta = 1.e-4
  solution_accuracy = 1.e-10
  exploratory_moves basic_pattern
  verbose output
method,
  id_method = 'NLP'
  model_pointer = 'M2'
  optpp newton
  gradient_tolerance = 1.e-12
  convergence_tolerance = 1.e-15
  verbose output
model,
  id_model = 'M1'
  single
  variables_pointer = 'V1'
  interface_pointer = 'I1'
  responses_pointer = 'R1'
model,
  id_model = 'M2'
  single
  variables_pointer = 'V1'
  interface_pointer = 'I1'
  responses_pointer = 'R2'
variables,
  id_variables = 'V1'
  continuous_design = 2
  initial_point 0.6 0.7
  upper_bounds 5.8 2.9
  lower_bounds 0.5 -2.9
  descriptors 'x1' 'x2'
interface,
  id_interface = 'I1'
  direct
  analysis_driver= 'text_book'
responses,
  id_responses = 'R1'
  num_objective_functions = 1
  no_gradients
  no_hessians
responses,
  id_responses = 'R2'
  num_objective_functions = 1
  analytic_gradients
  analytic_hessians
```



Evolutionary Algorithm:
*Generates Multiple Starting Points
for Pattern Search*



Pattern Search Ensemble:
*Generates Starting Point
for Newton Method to finish*

Newton Method

Multi-Objective Optimization

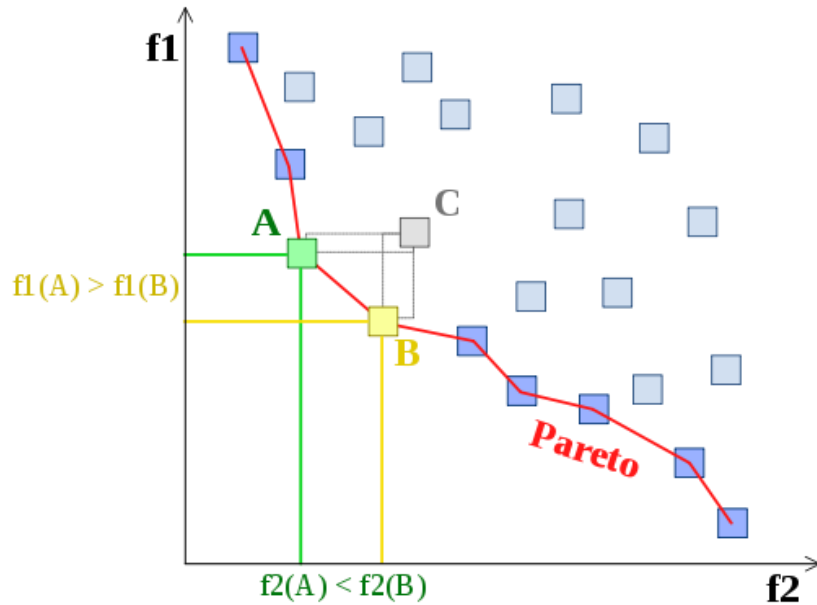


Image from http://en.wikipedia.org/wiki/Pareto_efficiency

May want tradeoffs between multiple objectives.

```
strategy,  
  single_method  
  tabular_graphics_data  
method,  
  optpp_q_newton  
  output verbose  
  convergence_tolerance = 1.e-8  
variables,  
  continuous_design = 2  
  initial_point      0.9    1.1  
  upper_bounds       5.8    2.9  
  lower_bounds       0.5   -2.9  
  descriptors        'x1'   'x2'  
interface,  
  system asynchronous  
  analysis_driver= 'text_book'  
responses,
```

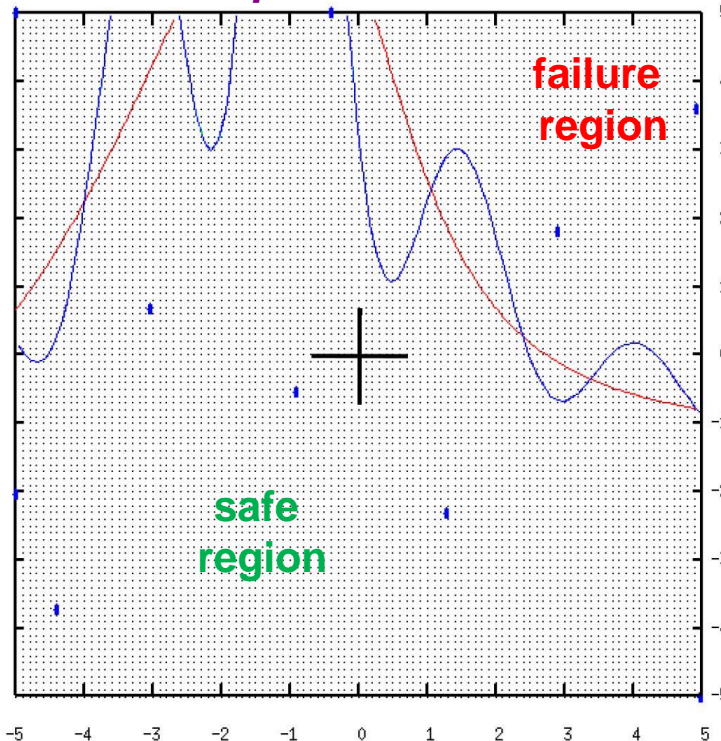
```
num_objective_functions = 3  
multi_objective_weights = .7 .2 .1  
analytic_gradients  
no_hessians
```


Efficient Global Reliability Analysis: GP Surrogate + MMAIS (B.J. Bichon)

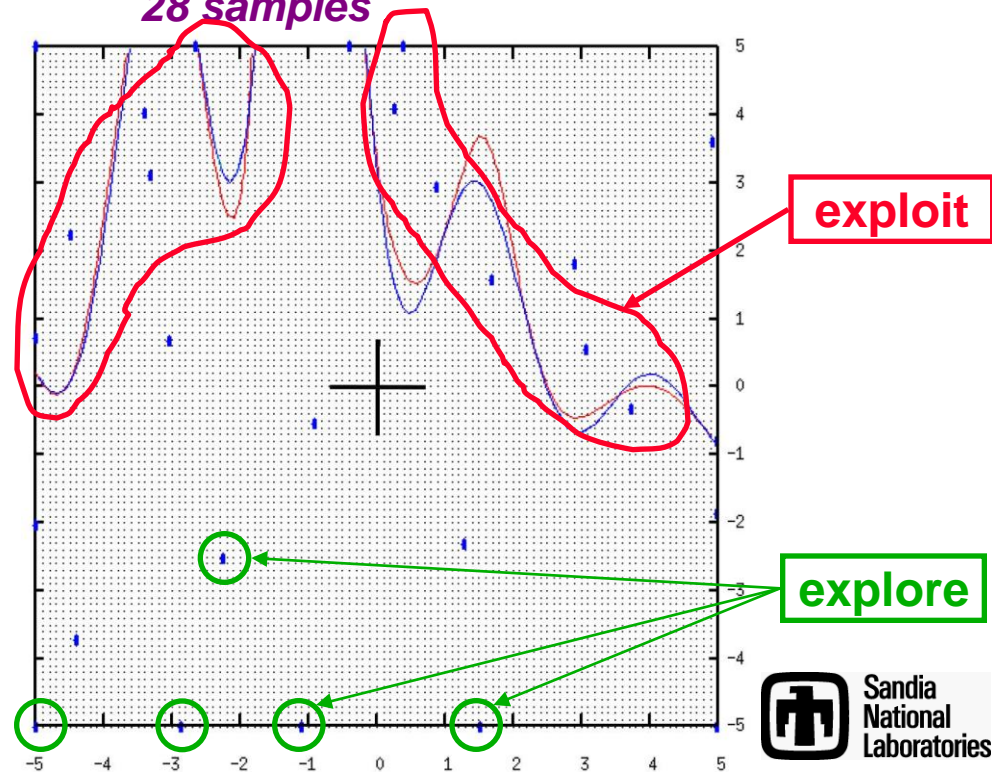


- Apply an EGO-like method to the equality-constrained optimization problem
- In EGRA, an expected feasibility function balances exploration with local search near the failure boundary to refine the GP
- Cost competitive with best MPP search methods, yet better probability of failure estimates; addresses nonlinear and multimodal challenges

*Gaussian process model (level curves) of reliability limit state with
10 samples*



28 samples

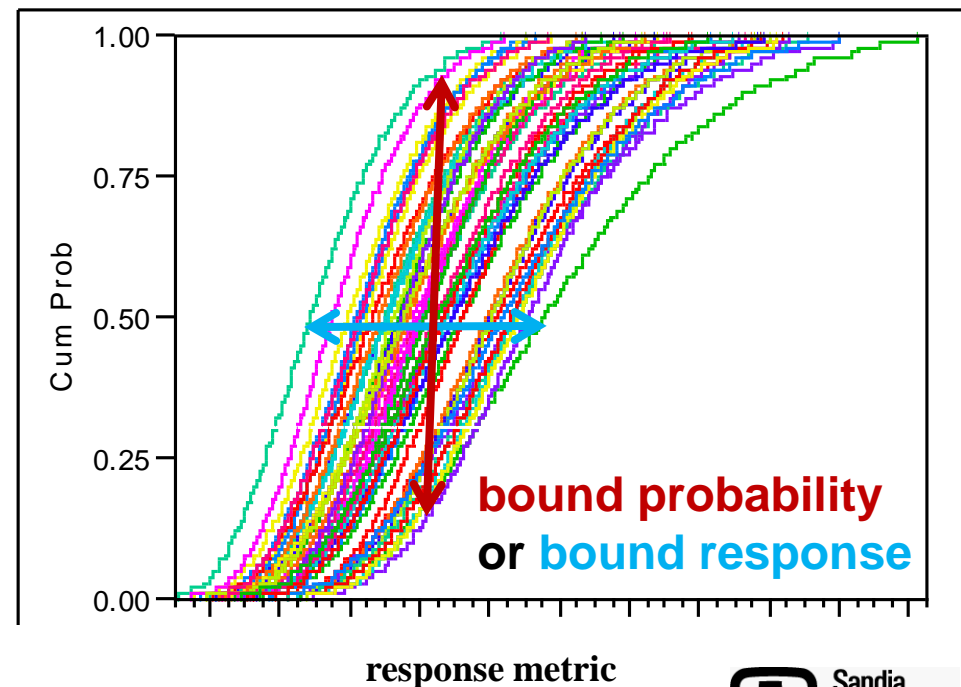
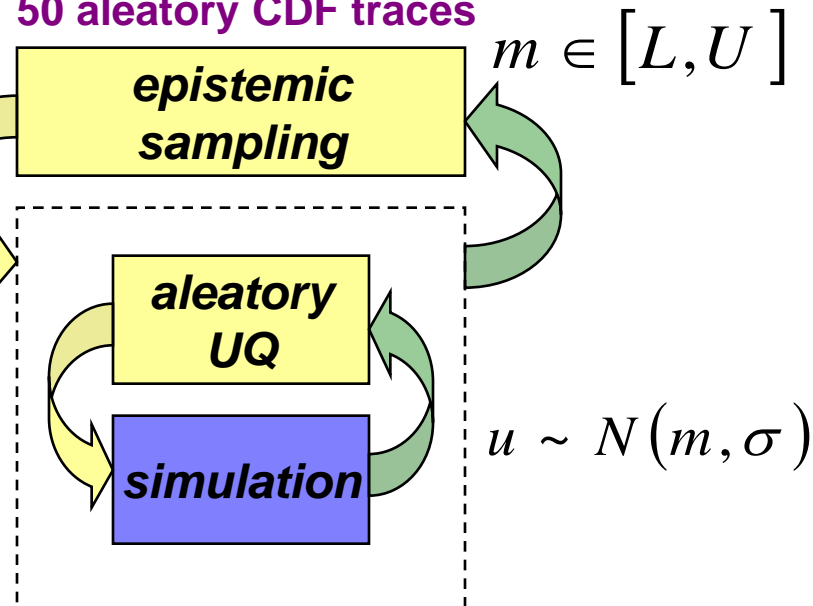


Epistemic UQ: Nested (“Second-order”) Approaches



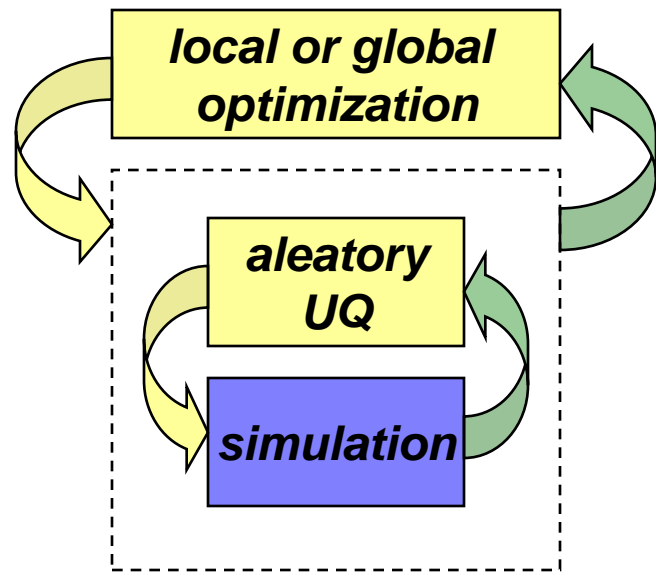
- Propagate over epistemic and aleatory uncertainty, e.g., **UQ with bounds on the mean of a normal distribution (hyper-parameters)**
- Typical in regulatory analyses (e.g., NRC. WIPP)
- Outer loop: epistemic (interval) variables, inner loop UQ over aleatory (probability) variables; **potentially costly, not conservative**
- ***If treating epistemic as uniform, do not analyze probabilistically!***

50 outer loop samples:
50 aleatory CDF traces



“Envelope” of CDF traces represents response epistemic uncertainty

Interval Estimation Approach (Probability Bounds Analysis)



- *Propagate intervals through simulation code*
- **Outer loop:** determine interval on statistics, e.g., mean, variance
 - global optimization problem: find max/min of statistic of interest, given bound constrained interval variables
 - use EGO to solve 2 optimization problems with essentially one Gaussian process surrogate
- **Inner loop:** Use sampling, PCE, etc., to determine the CDFs or moments with respect to the aleatory variables

$$\min_{u_E} f_{STAT}(u_A | u_E)$$

$$u_{LB} \leq u_E \leq u_{UB}$$

$$u_A \sim F(u_A; u_E)$$

$$\max_{u_E} f_{STAT}(u_A | u_E)$$

$$u_{LB} \leq u_E \leq u_{UB}$$

$$u_A \sim F(u_A; u_E)$$

Many Types of Data-Fit Surrogates



Polynomials are accurate in small regions and smooth noisy data.

linear

$$\hat{f}(\mathbf{x}) \approx c_0 + \sum_{i=1}^n c_i x_i$$

quadratic

$$\hat{f}(\mathbf{x}) \approx c_0 + \sum_{i=1}^n c_i x_i + \sum_{i=1}^n \sum_{j \geq i}^n c_{ij} x_i x_j$$

cubic

$$\hat{f}(\mathbf{x}) \approx c_0 + \sum_{i=1}^n c_i x_i + \sum_{i=1}^n \sum_{j \geq i}^n c_{ij} x_i x_j + \sum_{i=1}^n \sum_{j \geq i}^n \sum_{k \geq j}^n c_{ijk} x_i x_j x_k$$

Splines can represent complex multi-modal surfaces and smooth noisy data.

$$\hat{f}(\mathbf{x}) = \sum_{m=1}^M a_m B_m(\mathbf{x})$$

truncated power basis functions

Gaussian processes are good predictors of mean and variance but can suffer from ill conditioning.

$$\hat{f}(\underline{x}) \approx \underline{g}(\underline{x})^T \underline{\beta} + \underline{r}(\underline{x})^T \underline{R}^{-1} (\underline{f} - \underline{G} \underline{\beta})$$

trend

correlation

Correction terms can be applied to surrogates for improved accuracy.

additive

$$\hat{f}_{hi_\alpha}(\mathbf{x}) = f_{lo}(\mathbf{x}) + \alpha(\mathbf{x})$$

multiplicative

$$\hat{f}_{hi_\beta}(\mathbf{x}) = f_{lo}(\mathbf{x}) \beta(\mathbf{x})$$

convex combination

$$\hat{f}_{hi_\gamma}(\mathbf{x}) = \gamma \hat{f}_{hi_\alpha}(\mathbf{x}) + (1 - \gamma) \hat{f}_{hi_\beta}(\mathbf{x})$$



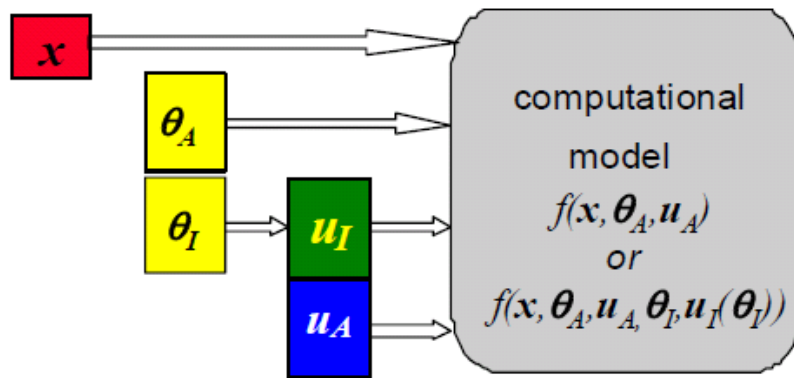
Parameter Estimation Topics



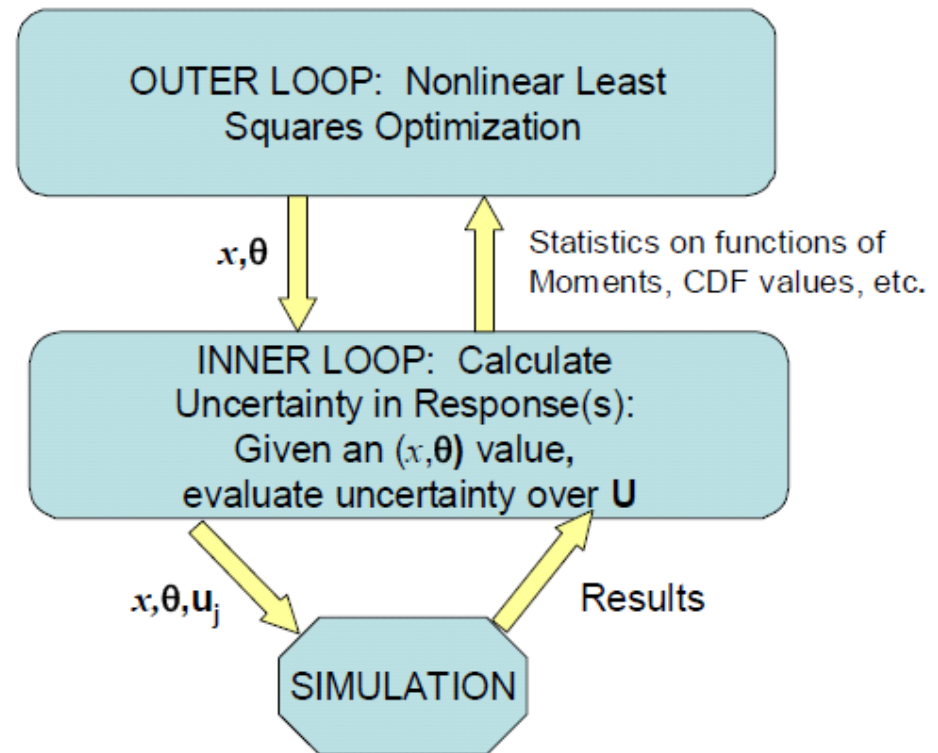
What are the challenges you face in calibration?

- Dealing with multiple data sets
- Data processing and interpolation
- Relevant metrics, statistics for comparing
- Calibration vs. validation
- Tools that would help your process

Calibration Under Uncertainty



Goal is now to match statistical moments of model over uncertain parameters with statistical moments of target.



Requires a nested solution approach.

Various Calibration Under Uncertainty Problems

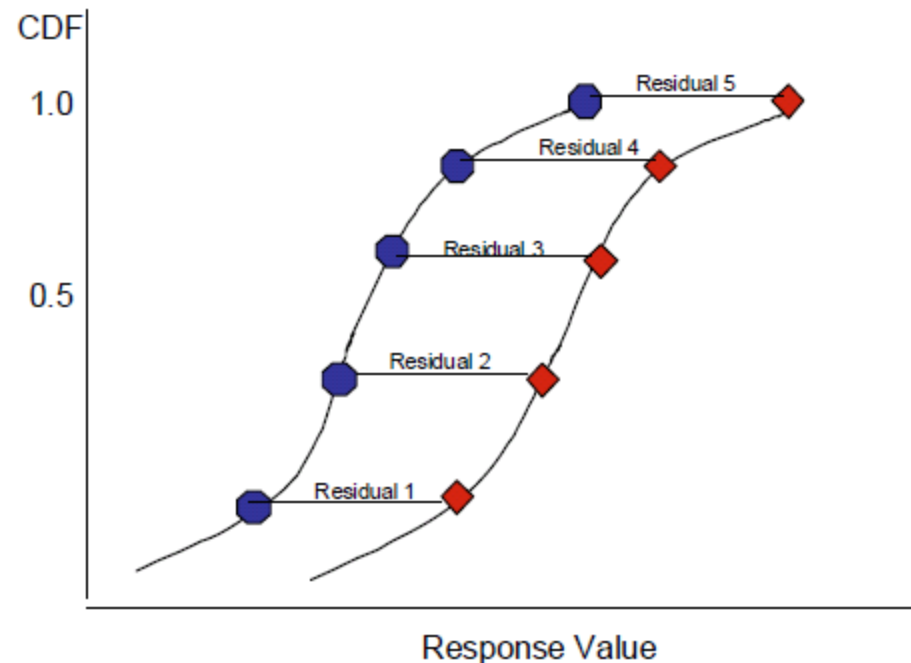
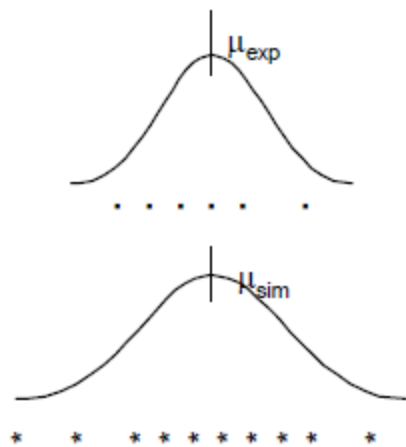


Matching Means

$$S(\theta) = (\mu_{\text{exp}} - \mu_{\text{sim}})^2 = \left(\frac{\sum_{i=1}^n y_i}{n} - \frac{\sum_{j=1}^m f(\mathbf{x}; \theta; u_j)}{m} \right)^2$$

Matching Means and Variances

$$S(\theta) = (\mu_{\text{exp}} - \mu_{\text{sim}})^2 + (\sigma_{\text{exp}} - \sigma_{\text{sim}})^2$$



Matching Distributions

$$S(\theta) = \sum_{k=1}^K (CDF_{\text{exp}(k)} - CDF_{\text{sim}(k)})^2 = \sum_{k=1}^K ([Y_k : \Pr(y \leq Y_k) = p_k] - [f_k : \Pr(f(\mathbf{x}; \theta; U) \leq f_k) = p_k])^2$$

$$S(\theta) = \sum_{k=1}^K (CDF_{\text{exp}(k)} - CDF_{\text{sim}(k)})^2 = \sum_{k=1}^K (\Pr(y \leq Y_k) - \Pr(f(\mathbf{x}; \theta; U) \leq Y_k))^2$$



Possible Advanced Topics (dictated by class interest)



General features

- Restart
- Evaluation cache
- Utilities in dakota_restart_util
- Tabular graphics data
- Failure capturing: abort, retry, recover, ignore
- Constraint specification: linear, nonlinear; equality, inequality
- Input/output scaling
- Matlab interface

Approximation methods

- Global data fit surrogate methods (polynomials, MARS, Kriging, etc.)
- Local surrogate methods (Taylor series, multipoint)
- Hierarchical: high/low fidelity models
- Corrections

Strategies/Advanced approaches

- Nested models: OUU
- Multi-objective (Pareto) optimization
- Multistart; multi-level hybrid
- Surrogate-based optimization (variety of constraint handling approaches): trust region; EGO/EGRA
- Reliability-based design optimization
- Advanced UQ topics: polynomial chaos, second-order probability, Dempster-Shafer, surrogate-based UQ
- AMPL: for analytic problems / algebraic mappings

Parallel capabilities: message passing, asynchronous local, hybrid

- Asynchronous evaluations
- Dakota parallel, application serial
- Dakota serial, application parallel
- Multi-level parallel: concurrent iteration, concurrent function evaluations, concurrent analyses,
- multiprocessor simulations

Getting Started and Getting Help



- Access a Sandia installation: `module avail dakota`
AMECH (CA), CEE (ESHPC/SCICO, NM), Computer clusters (both)
or download
- Supported on Linux/Unix, Mac OS X,
Windows (no MinGW or Cygwin install required)
- Tour DAKOTA web pages: <http://dakota.sandia.gov>
 - Extensive documentation (*user, reference*, developer)
 - Support mailing lists / archives
 - Software downloads: official releases and nightly stable
(freely available worldwide via GNU GPL)
- *User's Manual, Chapter 2*: Tutorial with example input files
- Support:
 - `dakota-users@software.sandia.gov`
(DAKOTA team and internal/external user community)
 - `dakota-help@sandia.gov`
(for SNL-specific or issues involving proprietary information)



Course Learning Goals: Did we meet them?



- Understand tools available in DAKOTA and the kind of design and analysis processes they can support
- Requirements for getting started
- See the mechanics of running DAKOTA
- Where to get help using DAKOTA
- *What pieces are still missing or unclear?*